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Using response surface design to determine the optimal parameters of genetic algorithm and a case study

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Genetic algorithms (GAs) are efficient stochastic search techniques for approximating optimal solutions within complex search spaces and used widely to solve NP-hard problems. Genetic algorithm includes a number of parameters whose different levels strictly affect the performance of the algorithm. The general approach to determine the appropriate parameter combination of GA depends on too many trials of different combinations, and the best one of them that produces good results is selected for the programme, which would be used for problem solving. A few researchers studied on the parameter optimisation of GA. In this paper, response surface-dependent parameter optimisation is proposed to determine the optimal parameters of GA. Results are tested for benchmark problems that are most common in mixedmodel assembly line balancing problems of type-I.

Keywords: Genetic algorithm (GA); Response surface methodology (RSM); Assembly line balancing; Parameter optimisation; Design of experiment

1. Introduction

Genetic algorithms (GAs) are part of the so-called evolutionary algorithms based on natural genetics that provide robust search capabilities in complex spaces, and thereby they offer a valid approach to problems requiring efficient and effective search processes. The basic idea is to maintain a population of individuals those representing candidate solutions to the problem that evolves over time through a process competition and they do not need to have any information about the search space, just needing a fitness function that assigns a value to each solution (Costa, Maciel, and Filho 2005; Fernandez-Prieto et al. 2011).

The running principle of GA depends on setting up of a relatively large number of parameters and requires performing lots of runs for different combinations of them to obtain the most appropriate structure that gives nearly optimal solution. There are few researches about parameter optimisation of GAs. Lobo and Goldberg (2004) presented the parameter-less GA to simplify GA operation by incorporating knowledge of parameter selection and population-sizing theory in the GA and applied it to a network expansion problem. Siriwardene and Perera (2006) used proportionate and linear ranking selection methods to determine model parameter convergence and recommended the proportionate selection method for urban drainage model parameter optimisation. Fernandez-Prieto et al. (2011) used fuzzy logic to determine GA control parameters (fuzzy adaptive genetic algorithms – FAGAs).

Taguchi experimental design is one of the well-known and effective experimental techniques that requires less experiment, and is used to find the best combination of parameters. Yang et al. (2005) combined the Taguchi experimental method with the GA to find the best combination of the GA parameters. One disadvantage of Taguchi method is that it does not give the mathematical model of the relations between parameters; so, predicting the intermediate values is impossible. Subbaraj, Rengaraj, and Salivahanan (2011) proposed a new optimisation algorithm, namely Taguchi selfadaptive real-coded GA and implemented it to solve economic dispatch problem with valve-point loading. Chang (2011) used Taguchi method to determine the important parameters in GA neural networks, with the goal of reducing the estimation error. The second one in the design of experiment techniques is the factorial design. This technique is used to model the non-quadratic relations between the factors and the response. The third and the widely used well-known design of experiment technique is the response surface methodology (RSM), which is based on statistical considerations that brings the most meaningful information about the influences of parameters on a specific problem, and process optimisation using RSM is usually achieved by simultaneous testing of numerous factors in a limited

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number of experiments. Therefore, RSM consumes less time and effort (Bayhan and Onel 2010; Costa, Maciel, and Filho 2005). Remarkable studies in the literature on this subject began with Pongcharoen et al. (2002). In this study, the authors performed a *factorial experiment* to identify appropriate values of GA parameters that produce the best results within a given execution time and developed a genetic algorithm-based scheduling tool (GAST) for scheduling of complex products with multiple resource constraints and deep product structure. Costa, Maciel, and Filho (2005) applied fractional factorial design for the selection of the parameters of GA and applied the GA to a batch cooling crystallisation optimisation. The brief literature review is summarised in Table 1.

According to Table 1, it is clearly observed that the studies on determining optimal parameter combination of GAs are limited, and response surface optimisation is not used for determining optimal GA parameters. In the present study, mixed-model assembly line balancing problem of type-I (MMALBP-I) is handled for a benchmark problem (test problem 8), which is taken from Simaria (2006), and the regression equation and optimum parameters calculated by response surface optimiser of Minitab-16 package is presented. Then, the experimental study is extended for the benchmark problems. When we reviewed the literature, we observed that RSM is not used for this purpose. The originality of this work is the application of RSM to the parameter optimisation of GA for MMALBP-I.

The rest of the paper is organised as follows. The concept and formulations of GA, RSM and MMALBP-I are presented in Section 2. An illustrative example is solved in Section 3. Discussions are given with the obtained results of test problems in Section 4 and conclusions are given in Section 5.

2. Proposed GA

GAs are powerful and broadly applicable random search and optimisation techniques, based on the principles of evolution theory. In recent years, GAs have been known to be extremely efficient for solving NP-hard problems (Zaman, Paul, and Azeem 2012). The following subsections describe in detail the features of the GA which are used in this research.

In the algorithm, we used task-based representation, which was used by Leu, Matheson, and Rees (1994), Sabuncuoglu and Tanyer (2000) and Akpinar and Bayhan (2011), since that is the most appropriate chromosome type for line balancing problems. The length of the chromosome is defined by adding two genes to the number of tasks. These two genes represent the station number and fitness value (FV) at the end of each chromosome. In task-based sequences, the chromosomes need to fit the precedence relationship diagram because of the technological precedence restrictions. Therefore, permutation coding method was used to sequence the tasks on the chromosomes without any repetition.

Random initialisation method, which initialises each chromosome randomly, was used to produce starting population. Initialisation method was specified in order to prevent unsuitable chromosomes, which interrupt precedence relationships.

GA used in this research employs the objective function given in Equation (1) as the fitness function to evaluate each individual's performance measure (fitness) in the search space.

$$
\text{Fitness Value} = \sum_{k=1}^{S} \frac{(C - W_k)^2}{S} \tag{1}
$$

Table 1. An overview of approaches in the literature on parameter optimisation of GAs.

Publications	Method	Problem
Pongcharoen et al. (2002)	Factorial design, regression analysis	Scheduling of complex products with multiple resource constraints
Lobo and Goldberg (2004)	Parameter-less genetic algorithm	Network expansion problem
Costa, Maciel, and Filho (2005)	2^{k-1} fractional factorial design	Batch cooling crystallisation optimisation
Siriwardene and Perera (2006)	Proportionate selection, linear ranking selection	Urban drainage model parameter optimisation
Yang et al. (2005)	Taguchi	Flight control design
Chang (2011)	Taguchi	Obtaining the steady state output voltage of proton exchange membrane fuel cell (PEMFC)
Fernandez-Prieto et al. (2011)	Fuzzy adaptive genetic algorithms – FAGAS	Computer networks under traffic loads
Subbaraj, Rengaraj, and Salivahanan (2011)	Taguchi self-adaptive real-coded genetic algorithm (TSARGA)	Economic dispatch problem

where C, W_k and S denote the cycle time of the assembly line, workload of the station k and the number of workstations required to meet the demand in the assembly line, respectively.

Individuals are selected randomly for mating. Thus, diversity is to be protected and probable better solutions can be occurred with the mating of worse individuals.

Two-point crossover method was used to perform the crossover operator according to the predefined crossover rate (C_R) . For mating, the individuals are selected randomly and paired with the other individuals.

The mutation operator exchanges randomly selected two genes according to the mutation rate (M_R) in a chromosome that is selected randomly. After the crossover and mutation operators, FVs of the new offspring are compared with the individuals' and the ones that have better FVs are transferred to next generation.

Elitism operator is applied indirectly by ensuring that none of the best individuals are missed during the iterations.

New generation is formed by selecting the best individuals according to their FVs among the current population, offspring produced by crossover and individuals who underwent mutation. Population size is kept constant by replacing the worse individuals with new ones by taking into account the FVs.

Repairing operator is not used in this algorithm since unsuitable chromosomes are not allowed to produce during the initialisation, crossover and mutation processes. Figure 1 shows the flow chart of GA used in this research.

2.1 Assembly line balancing problem

Assembly line balancing problem has received significant attention in the literature over five decades since it was first formulated by Salveson (1955) (Hamzadayi and Yildiz 2012). An assembly line consists of a number of workstations linked together with a material handling system, such as conveyor or moving belt (Azzi et al. 2012). The most common and difficult problem is to determine how these tasks can be assigned to the stations fulfilling certain restrictions, since the manufacturing process is divided into a set of tasks. So, the main objective is to determine optimal assignment of the tasks to the workstations (Chica et al. 2012).

Figure 1. Flow chart of proposed GA.

There are three types of MMALBP in the literature, and these are classified according to their objective functions. The types of the MMALBP are (Scholl 1995):

- MMALBP-I: The number of workstations is to be minimised for a given cycle time.
- MMALBP-II: The cycle time is to be minimised for given number of workstations.
- MMALBP-E: The cycle time and the number of workstations are to be minimised simultaneously.

The objective function used as fitness function of GA (Equation (1)) was taken from Leu, Matheson, and Rees (1994). This function minimises not only total number of workstations, but also helps workload smoothing between the workstations at the same time.

The decision variables x_{ik} and r_k check whether the task i is assigned to the workstation k and if the workstation k is replicated or not, respectively.

$$
x_{ik} = \begin{cases} 1, & \text{if task } i \text{ is assigned to workstation } k, \\ 0, & \text{otherwise} \end{cases}
$$

$$
r_k = \begin{cases} 1, & \text{if workstation } k \text{ is replicated,} \\ 0, & \text{otherwise} \end{cases}
$$

Assumptions of the model are (Akpinar and Bayhan 2011; Vilarinho and Simaria 2002):

- \bullet the planning horizon has a fixed length P ,
- \bullet a set of similar M models can be simultaneously assembled,
- the forecast demand, over the planning horizon, for model m is D_m , requiring the line to be operated with a cycle time;

$$
C = P / \sum_{m=1}^{M} D_m \tag{2}
$$

 \bullet the overall proportion of the number of units of model *m* being assembled is then:

$$
q_m = D_m / \sum_{p=1}^{M} D_p \tag{3}
$$

(where D_p describes the amount of total production for all models)

- each model has its own set of precedence relationships; but, there is a subset of tasks common to all models. Hence, the precedence diagrams for all the models can be combined and the resulting one has N tasks,
- N tasks are performed in a set of S workstations,
- the time required to perform task i on model m, t_{im} , may vary among models ($t_{im} = 0$ means that model m does not require task i to be assembled),
- a task can be assigned to only one workstation, and consequently the tasks that are common to several models need to be performed at the same workstation,
- the set of tasks that cannot be performed before task i is completed, F_i (successors of task i), is given by the precedence constraints derived from the combined precedence diagram,
- \bullet the zoning constraints are defined in the assembly process, ZP is the set of task pairs that must be assigned to the same workstation (compatible tasks) and ZN is the set of task pairs that cannot be performed at the same workstation (incompatible tasks),
- a workstation can be duplicated upto a maximum of MAXP replicas, but only if the task time of one of the tasks assigned to it exceeds a predefined value (α % of the cycle time) for at least one of the models (for our model $MAXP = 2$),

• S_{km} symbolises the idle time of workstation k for model m.

Constraints considered in the model are (Vilarinho and Simaria 2002):

$$
\sum_{k=1}^{S} x_{ik} = 1 \quad i = 1, ..., N
$$
 (4)

$$
\sum_{k=1}^{S} x_{ak} - \sum_{k=1}^{S} x_{bk} \le 0 \quad a \in N, \ b \in F_a \tag{5}
$$

$$
\sum_{k=1}^{S} x_{ak} - \sum_{k=1}^{S} x_{bk} = 0 \ (a, b) \in ZP \tag{6}
$$

$$
x_{ak} + x_{bk} \le 1 \ (a, b) \in ZN, \ k = 1, \dots, S \tag{7}
$$

$$
\sum_{i=1}^{N} t_{im} x_{ik} + S_{km} = C[1 + r_k(MATP - 1)] \quad k = 1, ..., S, \ m = 1, ..., M
$$
 (8a)

$$
r_k \leq \sum_{i:\exists t_{im} > \alpha C;\ m=1,\dots,M} x_{ik} \quad k=1,\dots,S, 0 < \alpha < 100\,\%
$$
 (8b)

$$
Mr_k \ge \sum_{i:\exists t_{lm} > \alpha C; m=1,\dots,M} x_{ik} \quad k=1,\dots,S, 0 < \alpha < 100\,\%
$$
\n(8c)

$$
S_{km} \geq 0 \quad k=1,\ldots,S, \ m=1,\ldots,M \tag{9a}
$$

$$
x_{ik} \in [0,1] \quad k = 1, \dots, S, \ i = 1, \dots, N \tag{9b}
$$

$$
r_k \in [0,1] \quad k=1,\ldots,S \tag{9c}
$$

The objective function (given in Equation (1)) minimises the sum of the squares of the idle times for each workstation; thus, it minimises not only the total number of workstations, but also the unbalanced workload between the workstations. Constraint (4) ensures that each task is assigned to exactly one workstation. Constraint (5) ensures none of the successors of a task are assigned to an earlier station than that task. Constraint (6) describes positive zoning constraints (compatibility zoning constraint). For instance, if any two tasks need to be performed at the same workstation because of technological restrictions, they must be assigned to same workstation. Constraint (7) describes negative zoning constraints (incompatibility zoning constraint). For example, if it is dangerous or impossible to perform any two tasks at the same workstation, they must be assigned to different workstations. Constraint (8a) ensures that the capacity is not exceeded for any workstation, constraint (8b) ensures that the maximum number of replicas of a workstation is not exceeded and constraint (8c) ensures that only workstations where the processing time of the tasks are assigned to it, for at least one model, exceeds a certain proportion (α %) of the cycle time can be duplicated (where M is a very large positive integer). Constraint (9a) describes the idle time of workstations equal or more than zero. Additionally, constraints (9b) and (9c) define the domain of the decision variables (Akpinar and Bayhan 2011; Vilarinho and Simaria 2002).

2.2 Response surface methodology

RSM is a union of statistical and mathematical techniques used for modelling mathematical relations between the inputs and outputs of a process, which is necessary for developing, improving and optimising processes. RSM has been used

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extensively in engineering problems to examine and characterise problems, in which input variables influence some performance aspects of the product or process. This performance measure is called as response. Product or process optimisation using RSM is usually achieved by simultaneous testing of numerous factors (controllable input variables) in a limited number of experiments. Therefore, RSM consumes less time and effort. Furthermore, RSM provides quantitative measurements of possible interactions between factors, difficult information to obtain using other optimisation techniques (especially by using heuristics). Detection and quantification of the interactions between various factors are important at the optimisation stage in engineering problems (Bayhan and Onel 2010). RSM was proposed by Box and Wilson (1951) for finding the input combination that minimises the output of a real non-simulated system. In most RSM problems, the form of the relationship between independent variables and the response is unknown and approximated (Dhupal, Doloi, and Bhattacharyya 2007). Equation (10) shows the general second-order polynomial response surface mathematical model (full quadratic model) for the experimental design (Dhupal, Doloi, and Bhattacharyya 2007; Yalcinkaya and Bayhan 2009).

$$
Y_u = \beta_0 + \sum_{i=1}^n \beta_i X_{iu} + \sum_{i=1}^n \beta_{ii} X_{iu}^2 + \sum_{i (10)
$$

where Y_u is the corresponding response, X_{iu} and X_{iu} are coded values of the *i*th and *j*th input parameters ($i < j$), respectively, the terms β_0 , β_i , β_{ii} and β_{ii} are the regression coefficients and e_u is the residual experimental error of the uth observation.

The model, in terms of the observations, may be written in matrix notation as (Montgomery 2001):

$$
Y = \beta X + \varepsilon \tag{11}
$$

where Y is the output matrix, X is the input matrix and ε is the matrix of residuals (error term). The least square estimator of β matrix that is comprised of coefficients of the regression equation is calculated by the given formula in Equation (12):

$$
\beta = (X'X)^{-1}X'Y\tag{12}
$$

The fitted regression models, with the coefficients for F^V are given in the next section.

3. Results

3.1 Parameter optimisation of GA

Randomised experimental runs were carried out to minimise the error. The factor levels of GA parameters for the experiments are generation number (G_N), population size (P_S), crossover rate (C_R) and mutation rate (M_R), which are listed in Table 2. The levels of these parameters are determined randomly by considering the levels from similar studies presented previously in the literature based on GA and MMALBP-I. Table 3 shows the experimental design, detailing the experiment run order of each experiment and coded values of the process parameters (namely factors). For each experiment, 100 runs are performed. Minitab-16 statistical software was used to establish mathematical models for optimisation of the GA parameters. The software uses the mathematical substructure given in Section 2.2.The RSM based mathematical model that represents the relations between the response FV and the factors G_N, P_S, C_R and M_R is established by considering the experimental design and given in Equation (13).

$$
FV = 10.0788 - 0.23994G_N - 0.43357P_S - 0.12353C_R - 0.09101M_R + 0.174854G_N^2 + 0.225179P_S^2
$$

+ 0.116204C_R² + 0.010491M_R² - 0.12087G_NP_S + 0.090719G_NC_R - 0.13349G_NM_R - 0.03798P_SC_R
- 0.02787P_SM_R - 0.02046C_RM_R

Optimisation procedure was performed to achieve the target value of FV, which is given in Equation (1). Optimum parameter settings obtained are presented in Figure 2.

The current coded optimal process parameter settings for achieving the targeted FV of $FV = 9$ are calculated as $G_N = 1.9596$, $P_S = 1.6364$, $C_R = 0.2222$ and $M_R = 2$. After the normalisation, the uncoded values are calculated as $G_N = 1039.9$, $P_S = 92.728$, $C_R = 0.5444$ and $M_R = 0.25$, respectively (Table 4). The response is optimised at the

		Level					
Parameter	Symbol	$^{-2}$	$\hspace{1.0cm} \rule{1.5cm}{0.15cm}$				
Generation number	G_N	50	300	550	800	1050	
Population size	P_{S}	20	40	60	80	100	
Crossover rate	C_R	0.1	0.3	0.5	0.7	0.9	
Mutation rate	M_R	0.05	0.1	0.15	0.2	0.25	

Table 2. Levels and values of GA parameters G_N , P_S , C_R , and M_R .

Table 3. Design of experiments matrix showing coded values and observed responses for 100 runs.

			Coded Value				
Experiment Number	Run Order	${\cal G}_{\cal N}$	${\cal P}_S$	$\mathcal{C}_\mathcal{R}$	$\mathcal{M}_{\mathcal{R}}$	Response Average ${\rm FV}$	
1		-1	-1	-1	-1	11.6584	
\overline{c}	\overline{c}		-1	-1	-1	10.7626	
3	3	- 1		-1	-1	10.4247	
4	4			-1	-1	9.9721	
5	5	- 1			-1	10.7962	
6	6		-1		-1	11.2854	
7	7	-1			-1	10.0964	
8	8				-1	10.4255	
9	9	-1				10.8994	
10	10		-1	— 1		11.2969	
11	11	— 1		-1		11.0452	
12	12			-1		9.6723	
13	13	-1	-1			11.5418	
14	14		-1			10.9198	
15	15	-1				10.4896	
16	16					9.4210	
17	17	-2	0	0	0	11.2915	
18	18	$\overline{2}$	$\overline{0}$	θ	$\overline{0}$	10.0103	
19	19	$\mathbf{0}$	-2	$\overline{0}$	$\overline{0}$	11.5502	
20	20	$\mathbf{0}$	\overline{c}	θ	$\overline{0}$	10.1542	
21	21	$\mathbf{0}$	$\boldsymbol{0}$	-2	$\boldsymbol{0}$	10.9685	
22	22	$\overline{0}$	$\mathbf{0}$	$\sqrt{2}$	$\overline{0}$	9.8641	
23	23	θ	$\boldsymbol{0}$	$\mathbf{0}$	-2	10.5057	
24	24	$\overline{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	\overline{c}	9.4812	
25	25	$\mathbf{0}$	$\boldsymbol{0}$	$\overline{0}$	$\boldsymbol{0}$	10.0597	
26	26	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	10.0849	
27	27	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	10.1023	
28	28	$\mathbf{0}$	$\boldsymbol{0}$	0	$\boldsymbol{0}$	10.1178	
29	29	$\mathbf{0}$	$\boldsymbol{0}$	0	$\boldsymbol{0}$	10.0195	
30	30	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	$\boldsymbol{0}$	10.0634	
31	31	$\boldsymbol{0}$	$\mathbf{0}$	$\mathbf{0}$	$\mathbf{0}$	10.1041	

above parametric combination with desirability (d) of 0.9912 (99.12%), and the optimised response value of FV is calculated as 9.0264 (see Figure 2).

The experimental results for the given case under this study are presented in the next section.

3.2 Experimental results for MMALBP-I

The GA was tested on a benchmark problem (test problem 8), given in Table 5, with the parameters found by RSM. The main characteristics of the most common test problems in the relevant literature are presented in Table 5 and the results compared with the previous results demonstrated in the literature for test problem 8 are shown in Table 6. To describe the problems, the number of tasks of the combined precedence diagram (N) , the number of models (M) and the cycle time of the assembly line (C) are given in the columns $3-5$ and $9-11$ in Table 5.

Figure 2. Optimisation results for G_N, P_S, C_R , and M_R .

Table 4. Results of parameter optimisation.

Symbol	Coded value	Uncoded value	Rounded value	
G_N	1.9596	1039.9	1040	
P_S	1.6364	92.73	93	
C_R	0.2222	0.54	0.50	
M_R		0.25	0.25	

Table 5. Test problems (Akpinar and Bayhan 2011; Scholl 1995; Vilarinho and Simaria 2002).

The precedence diagram (Figure 3) and task processing times used for the test problem 8 (with 25 tasks, 3 models) was taken from Simaria (2006). The coding of the GA was developed in Matlab R2008a and implemented on Intel Core i5 CPU M480 2.67 GHz system with 3 GB RAM and 64-bit operating system.

The computational results for the given test problem are presented in Table 6. LB_{pmix} column shows the lower bound on the total number of workstations for relevant problem (Vilarinho and Simaria 2002). The columns Kilbridge & Wester, Moodie & Young, RPWT and Pure GA (Akpinar and Bayhan 2011) show the best solutions in the relevant literature found by different solution approaches. V&S (SA) and A&B (hGA) columns represent the best solutions

Figure 3. Precedence diagram of test problem 8 (Simaria 2006).

Table 6. Computational results (station numbers) for test problem 8.

#	Problem	LB_{pmix}	Kilbridge $\&$ Wester	Moodie & Young (Phase I)	RPWT	Pure GA	V&S (SA)	A&B (hGA)	RSM-GA
8	Vilarinho and Simaria (2002)	-14				$\overline{}$			

found by Vilarinho and Simaria (2002), by using simulated annealing (SA) algorithm, and Akpinar and Bayhan (2011) by using hybrid genetic algorithm (hGA), respectively. RSM-GA column represents the best station number found by using optimised parameters of GA obtained from RSM. The task sequences discovered by RSM-GA procedure are given in appendices.

3.3 Comparisons for well-known design of experiment techniques

In this section, a comprehensive experimental design is performed to clearly show the advantage of using RSM instead of using other well-known design of experiment techniques. For this purpose, experimental designs are performed for the two well-known design of experiment technique, namely Taguchi method and 2^k factorial design.

It is well known in the literature that Taguchi method requires less experiment when compared with RSM; but, this method provides only the optimum combination of factor levels. So, RSM is more appropriate for this type of problem because it is possible with RSM to calculate the optimum factor levels with decimals, as can be seen in Table 4. In other words, it is possible to obtain more sensitive parameter levels with RSM when it is compared with the solutions of Taguchi method. The same sensitivity may also be obtained by 2^k factorial design; but, this technique depends on the first-order (linear) relations between the independent factors. The parameter optimisation case presented in this study shows nonlinear relations because of the nature of the problem. So, 2^k factorial design does not seem a good alternative to the RSM. The factor levels for Taguchi method and 2^k factorial design are presented in Tables 7 and 10, and the simulation results for the given experimental designs are presented in Tables 8 and 11 respectively.

By using the five-level design of Taguchi for four factors, the design composed of 25 experiments is obtained and displayed in Table 8, and the average FV values are calculated for each parameter combination.

Parameter				Level		
	Symbol					
Generation number	G_N	50	300	550	800	1050
Population size	P_{S}	20	40	60	80	100
Crossover rate	C_R	0.1	0.3	0.5	0.7	0.9
Mutation rate	M_{R}	0.05	0.1	0.15	0.2	0.25

Table 7. Factor levels and values of GA parameters for Taguchi design.

			Coded value				
Experiment number	Run order	${\cal G}_N$	${\cal P}_S$	$\mathcal{C}_\mathcal{R}$	$\mathcal{M}_{\mathcal{R}}$	Response Average FV	
						12.8754	
2					2	10.2845	
3						10.3232	
4						10.0746	
5						10.0551	
6						12.5041	
7				3		11.6579	
8						9.7338	
9	9	2				10.0792	
10	10	2				9.2989	
11	11	3				12.4054	
12	12					10.9296	
13	13					10.2612	
14	14					11.1595	
15	15					9.7173	
16	16					12.5572	
17	17					10.496	
18	18		3			9.6257	
19	19					10.9025	
20	20					10.1299	
21	21					12.4396	
22	22					10.1224	
23	23		3			10.9064	
24	24					10.8023	
25	25	5	5		3	10.1464	

Table 8. Taguchi design and simulation results for average FV.

For the optimisation, smaller is better criterion of Taguchi method is used. For minimising average FV; Signal to Noise (S/N) ratios for each experimental runs are calculated from Minitab. Minitab uses the formula given below in Equation (14) to calculate S/N ratios for smaller is better criteria:

$$
S/N = -10\left(\log\left(\sum Y^2/n\right)\right) \tag{14}
$$

Calculated signal to noise (S/N) ratios for smaller is better criteria are listed in Table 9. The factor level that has the maximum S/N ratio for each factor is selected as the optimum factor level for the factors and is given in bold.

Table 9. Signal to noise (S/N) ratios for smaller is better criteria.

Level	G_N		C_R	M_R
	-20.57	-21.98	-20.46	-20.78
2	-20.5	-20.57	-20.69	-20.5
3	-20.71	-20.14	-20.85	-20.74
4	-20.59	-20.5	-20.54	-20.54
5	-20.71	-19.88	-20.53	-20.51

Table 10. Factor levels and values of GA parameters for 2^k factorial design.

Experiment number			Coded value				
	Run order	G_N	P_S	C_R	M_R	Response Average FV	
			$\overline{}$	-1	-1	13.9733	
$\mathcal{D}_{1}^{(1)}$						12.3377	
3						9.9266	
4					$\overline{}$	10.9129	
5						13.4973	
6						11.2922	
						9.7846	
8						11.8925	
9						12.9618	
10	10			$\overline{}$		9.7963	
11	11					9.4492	
12	12					9.6476	
13	13					11.7615	
14	14					13.8808	
15	15					10.3125	
16	25					10.2736	

Table 11. 2^k factorial design and simulation results for average FV.

According to the S/N ratios, optimum coded parameter combination is found as $G_N(2)$, $P_S(5)$, $C_R(1)$ and $M_R(2)$. The uncoded levels are calculated as $G_N(300)$, $P_S(100)$, $C_R(0.1)$, and $M_R(0.1)$.

Another well-known design of experiment technique is the 2^k factorial design, as mentioned previously. The factor levels for 2^k design are determined as given in Table 10. By using the two-level factorial design for the four factors, the design composed of 16 experiments is obtained and displayed in Table 11, and the average FVs are calculated for each parameter combination.

Mathematical model was based on 2^k factorial design for correlating responses, such as the parameters. G_N , P_S , C_R and M_R , with various settings of the process parameters considered in the experimental design, have been established and is represented in the Equation (15) as follows:

Figure 4. Optimisation results for the G_N, P_S, C_R and M_R for 2^k factorial design.

$$
FV = 11.3563 - 0.1021G_N - 1.0813P_S + 0.2306C_R - 0.3459M_R + 0.5088G_NP_S + 0.3500G_NC_R - 0.0088G_NM_R
$$

+ 0.0603P_SC_R - 0.0084P_SM_R + 0.3161C_RM_R - 0.2394G_NP_SC_R - 0.3581G_NP_SM_R + 0.2810G_NC_RM_R
- 0.235P_SC_RM_R - 0.4508G_NP_SC_RM_R (15)

Optimisation analysis was performed to achieve the target value of FV that is given in Equation (1). Obtained optimum parameter settings are presented in Figure 4.

The current coded optimal process parameter settings for achieving the targeted FV of $FV = 9$ are $G_N(-1), P_S(1), C_R(-1),$ and $M_R(1)$. The uncoded values are calculated as $G_N(50), P_S(100), C_R(0.1)$ and $M_R(0.25)$, respectively. The response is optimised at the above parametric combination with desirability (d) of 0.5508 (55.08%), and optimised response value of FV is calculated as 9:4492.

The computational results (station numbers) for test problem 8 with the optimum parameter levels are calculated as 15 stations for both Taguchi method and 2^k factorial design. Results indicate that RSM is more efficient with 14 stations as mentioned before in Table 6.

4. Discussion

As can be seen from Table 6, GA, with proposed parameters calculated by using RSM, has found 14 work stations for test problem 8 and this result is equal or better than previous works for medium-sized benchmark problem of Vilarinho and Simaria (2002). Furthermore, for the mentioned test problem, obtained solution by proposed method in this paper is equal to the theoretical lower bound of total workstations (LB_{pmix}). Results demonstrate that without using any hybridisation, the obtained solution by only optimising the parameters of pure GA with RSM is better than the solutions of Kilbridge & Wester, Moodie & Young (Phase I), RPWT, Pure GA and SA of Vilarinho and Simaria (2002). Additionally, the obtained result equals to the result obtained from hybrid GA of Akpinar and Bayhan (2011). The proposed GA parameters, which are given in Table 4, may be used as the best parameters set for test problem 8 for the future researches.

Similarly, further experiments are carried out to solve other MMALBP-I test problems in Table 5 using proposed procedures with optimised parameters. The obtained total number of required station numbers for each test problem is given in the RSM-GA column in Table 12.

#	Problem	LB_{pmix}	Kilbridge & Wester	Moodie & Young (Phase I)	RPWT	Pure GA	V&S (SA)	A&B (hGA)	$RSM-$ GA
P ₁	Bowman	4	4	4	4	4	4	4	4
P ₂	Bowman	6	9	9	9	8	8	8	8
P ₃	Gokcen and Erel (1998)	7	8		8	7	7	τ	
P4	Gokcen and Erel (1998)	6				7	7	$\overline{7}$	
P ₅	Mitchel	14	17	16	16	16	16	16	16
P ₆	Mitchel	13	16	15	17	15	15	15	15
P ₇	Vilarinho and Simaria (2002)	14	17	17	18	16	16	16	16
P8	Vilarinho and Simaria (2002)	14	15	15	15	15	15	14	14
P ₉	Heskiakof	19	21	21	21	21	21	20	20
P ₁₀	Heskiakof	18	21	21	21	20	20	20	20
P ₁₁	Sawyer	15	18	18	19	16	16	16	16
P12	Sawyer	17	21	21	20	19	19	19	19
P ₁₃	Lutz 1	16	19	19	19	19	19	19	19
P ₁₄	Lutz 1	17	21	20	20	19	19	19	19
P ₁₅	Gunther	20	25	25	24	24	24	23	24
P ₁₆	Gunther	21	26	26	25	25	24	24	24
P17	Kilbridge & Wester	23	27	27	28	25	25	25	25
P ₁₈	Kilbridge & Wester	24	31	29	29	28	28	27	27
P ₁₉	Tonge	41	50	48	48	45	44	44	44
P ₂₀	Tonge	39	48	47	48	45	44	44	45

Table 12. Comparison of obtained results (station numbers) for test problems.

Based on the results demonstrated in Table 12, it is clearly seen that the proposed method outperforms three traditional heuristics (Kilbridge & Wester, Moodie & Young – Phase I, RPWT) and Pure GA. The proposed method produces better solutions than Pure GA for five test problems, P8, P9, P16, P18 and P19. Moreover, equal solutions are observed for remaining test problems (P1–P7, P10–P15, P17 and P20). Hence, it can be said that RSM-GA may have a potential capacity to generate better solutions than Pure GA by only optimising its parameters without using any hybridisation.

In terms of comparison between SA algorithm (Vilarinho and Simaria 2002) and RSM-GA, better solutions are obtained for three test problems (P8, P9 and P18) while in tie for remaining problems, except P20. Furthermore, the found solutions are equal to hGA (Akpinar and Bayhan 2011) for 18 test problems, while worse than hGA for only P15 and P20.

To conclude, the present paper demonstrates that by using only RSM, it is possible to obtain better results. The advantage of using RSM in the present study is obtaining the acceptable results with only running 31 experiments with 100 runs (preferable number of runs may be lower than 100 if the CPU time is quite high) for the given case without using any hybridisation.

While RSM appears to be quite useful for analysing many simulation problems, it has not received much attention from practitioners, despite efforts to encourage its application (Safizadeh and Thornton 1984). The results of this study showed one more time that the RSM is an efficient statistical technique necessary for developing, improving and optimising processes. The application of RSM is quite easy when compared with the other hybridisations mentioned in the literature. This may provide convenience to the researchers.

5. Conclusions

The aim of this paper is to search the effect of parameter optimisation on GAs' performance. For this purpose, RSM is applied to average FVs of 100 replicates of different parameter combinations for the test problem of Vilarinho and Simaria (2002) (problem 8, 25 tasks, 3 models, medium-sized problem of MMALBP-I) and best parameter combination is tried to find. By using the optimal parameters of GA, calculated by response optimiser, it was tested for the mentioned problem several times and 14 workstations with alternative task sequences are obtained. The objective was minimisation of number of workstations with balanced workload. By the proposed method, the probability of finding good solutions was increased by 6.67% ($(15 - 14)/15 = 0.067$) for the 8th test problem. Furthermore, a comprehensive experimental design is performed to see the advantages of RSM by comparing the results obtained from RSM with the Taguchi and 2^k factorial design methods. Then, to demonstrate the performance of the RSM-GA, 20 test problems from the literature (given in Table 5) are solved by using RSM-GA, and results are compared with existing results in the relevant literature. The results presented in this study obviously show that the proposed approach based on RSM can successfully be used for the fast and easy design of the optimal parameter levels of GA for MMALBP-I. Also, according to the results, it is clearly observed that the solution quality of the traditional GA was improved.

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Appendix 1. Obtained alternative solutions/task sequences (or chromosomes) for test problem 8 (25 tasks – 3 models) are given in following tables

Table A1. Alternative solution-1.

